

P.22 I.

$$(1) \left[\begin{array}{cc|c} 2 & 3 & -1 \\ 1 & -1 & 2 \end{array} \right] \xrightarrow{\textcircled{1} + \textcircled{2} \times (-2)} \left[\begin{array}{cc|c} 0 & 5 & -5 \\ 1 & -1 & 2 \end{array} \right] \xrightarrow{\textcircled{1} \times (\frac{1}{5})} \left[\begin{array}{cc|c} 0 & 1 & -1 \\ 1 & -1 & 2 \end{array} \right]$$

$$\xrightarrow{\textcircled{2} + \textcircled{1}} \left[\begin{array}{cc|c} 0 & 1 & -1 \\ 1 & 0 & 1 \end{array} \right] \xrightarrow{\textcircled{1} \leftrightarrow \textcircled{2}} \left[\begin{array}{cc|c} 1 & 0 & 1 \\ 0 & 1 & -1 \end{array} \right] \quad \therefore \begin{cases} x_1 = 1 \\ x_2 = -1 \end{cases}$$

$$(2) \left[\begin{array}{cc|c} 3 & 2 & 0 \\ 1 & -2 & 8 \end{array} \right] \xrightarrow{\textcircled{1} + \textcircled{2} \times (-3)} \left[\begin{array}{cc|c} 0 & 8 & -24 \\ 1 & -2 & 8 \end{array} \right] \xrightarrow{\textcircled{1} \times (\frac{1}{8})} \left[\begin{array}{cc|c} 0 & 1 & -3 \\ 1 & -2 & 8 \end{array} \right]$$

$$\xrightarrow{\textcircled{2} + \textcircled{1} \times 2} \left[\begin{array}{cc|c} 0 & 1 & -3 \\ 1 & 0 & 2 \end{array} \right] \xrightarrow{\textcircled{1} \leftrightarrow \textcircled{2}} \left[\begin{array}{cc|c} 1 & 0 & 2 \\ 0 & 1 & -3 \end{array} \right] \quad \therefore \begin{cases} x_1 = 2 \\ x_2 = -3 \end{cases}$$

$$(3) \left[\begin{array}{ccc|c} 1 & 2 & -1 & 2 \\ -1 & 0 & 3 & 8 \\ 0 & 1 & -2 & -4 \end{array} \right] \xrightarrow{\textcircled{1} + \textcircled{2}} \left[\begin{array}{ccc|c} 0 & 2 & 2 & 10 \\ -1 & 0 & 3 & 8 \\ 0 & 1 & -2 & -4 \end{array} \right] \xrightarrow{\textcircled{1} \times (\frac{1}{2})} \left[\begin{array}{ccc|c} 0 & 1 & 1 & 5 \\ -1 & 0 & 3 & 8 \\ 0 & 1 & -2 & -4 \end{array} \right]$$

$$\xrightarrow{\substack{\textcircled{1} - \textcircled{3} \\ \textcircled{2} \times (-1)}} \left[\begin{array}{ccc|c} 0 & 1 & 1 & 5 \\ 1 & 0 & -3 & -8 \\ 0 & 0 & -3 & -9 \end{array} \right] \xrightarrow{\textcircled{1} \times (-\frac{1}{3})} \left[\begin{array}{ccc|c} 0 & 1 & 1 & 5 \\ 1 & 0 & -3 & -8 \\ 0 & 0 & 1 & 3 \end{array} \right] \xrightarrow{\substack{\textcircled{1} - \textcircled{3} \\ \textcircled{2} + \textcircled{3} \times 3}} \left[\begin{array}{ccc|c} 0 & 1 & 0 & 2 \\ 1 & 0 & 0 & 1 \\ 0 & 0 & 1 & 3 \end{array} \right]$$

$$\xrightarrow{\textcircled{1} \leftrightarrow \textcircled{2}} \left[\begin{array}{ccc|c} 1 & 0 & 0 & 1 \\ 0 & 1 & 0 & 2 \\ 0 & 0 & 1 & 3 \end{array} \right] \quad \therefore x_1 = 1, x_2 = 2, x_3 = 3 //$$

$$(4) \left[\begin{array}{ccc|c} 1 & 1 & -1 & 1 \\ 2 & 1 & 3 & 4 \\ -1 & 2 & -4 & -2 \end{array} \right] \xrightarrow{\substack{\textcircled{2} - \textcircled{1} \times 2 \\ \textcircled{3} + \textcircled{1}}} \left[\begin{array}{ccc|c} 1 & 1 & -1 & 1 \\ 0 & -1 & 5 & 2 \\ 0 & 3 & -5 & -1 \end{array} \right] \xrightarrow{\substack{\textcircled{1} + \textcircled{2} \\ \textcircled{3} + \textcircled{2} \times 3}} \left[\begin{array}{ccc|c} 1 & 0 & 4 & 3 \\ 0 & -1 & 5 & 2 \\ 0 & 0 & 10 & 5 \end{array} \right]$$

$$\xrightarrow{\substack{\textcircled{2} \times (-2) \\ \textcircled{3} \times (\frac{1}{5})}} \left[\begin{array}{ccc|c} 1 & 0 & 4 & 3 \\ 0 & 2 & -10 & -4 \\ 0 & 0 & 2 & 1 \end{array} \right] \xrightarrow{\substack{\textcircled{2} + \textcircled{3} \times 5 \\ \textcircled{1} + \textcircled{3} \times (-2)}} \left[\begin{array}{ccc|c} 1 & 0 & 0 & 1 \\ 0 & 2 & 0 & 1 \\ 0 & 0 & 2 & 1 \end{array} \right] \xrightarrow{\substack{\textcircled{2} \times (\frac{1}{2}) \\ \textcircled{3} \times (\frac{1}{2})}} \left[\begin{array}{ccc|c} 1 & 0 & 0 & 1 \\ 0 & 1 & 0 & \frac{1}{2} \\ 0 & 0 & 1 & \frac{1}{2} \end{array} \right]$$

$$\therefore x_1 = 1, x_2 = \frac{1}{2}, x_3 = \frac{1}{2} //$$

P.22 2.

$$(1) \left[\begin{array}{ccc|c} 3 & 1 & -1 & -7 \\ 1 & -1 & 2 & 2 \end{array} \right] \xrightarrow{\textcircled{1}-3\times\textcircled{2}} \left[\begin{array}{ccc|c} 0 & 4 & -7 & -7 \\ 1 & -1 & 2 & 2 \end{array} \right] \xrightarrow{\textcircled{2}\times 4} \left[\begin{array}{ccc|c} 0 & 4 & -7 & -7 \\ 4 & -4 & 8 & 8 \end{array} \right] \xrightarrow{\textcircled{2}+\textcircled{1}} \left[\begin{array}{ccc|c} 0 & 4 & -7 & -7 \\ 4 & 0 & 1 & 1 \end{array} \right]$$

$$\xrightarrow{\textcircled{1}, \textcircled{2}\times(1/4)} \left[\begin{array}{ccc|c} 0 & 1 & -7/4 & -7/4 \\ 1 & 0 & 1/4 & 1/4 \end{array} \right] \xrightarrow{\textcircled{1}\leftrightarrow\textcircled{2}} \left[\begin{array}{ccc|c} 1 & 0 & 1/4 & 1/4 \\ 0 & 1 & -7/4 & -7/4 \end{array} \right] \quad \therefore \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} = \frac{1}{4} \begin{bmatrix} 1 \\ -7 \end{bmatrix}$$

$$(2) \left[\begin{array}{ccc|c} 3 & 5 & 2 & 2 \\ 1 & 3 & 0 & 0 \end{array} \right] \xrightarrow{\textcircled{1}-3\times\textcircled{2}} \left[\begin{array}{ccc|c} 0 & -4 & 2 & 2 \\ 1 & 3 & 0 & 0 \end{array} \right] \xrightarrow[\textcircled{2}\times 2]{\textcircled{1}\times(1/2)} \left[\begin{array}{ccc|c} 0 & 2 & -1 & -1 \\ 2 & 6 & 0 & 0 \end{array} \right] \xrightarrow{\textcircled{2}-3\times\textcircled{1}} \left[\begin{array}{ccc|c} 0 & 2 & -1 & -1 \\ 2 & 0 & 3 & 3 \end{array} \right]$$

$$\xrightarrow{\textcircled{1}, \textcircled{2}\times(1/2)} \left[\begin{array}{ccc|c} 0 & 1 & -1/2 & -1/2 \\ 1 & 0 & 3/2 & 3/2 \end{array} \right] \xrightarrow{\textcircled{1}\leftrightarrow\textcircled{2}} \left[\begin{array}{ccc|c} 1 & 0 & 3/2 & 3/2 \\ 0 & 1 & -1/2 & -1/2 \end{array} \right] \quad \therefore \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} = \frac{1}{2} \begin{bmatrix} 3 \\ -1 \end{bmatrix}$$

$$(3) \left[\begin{array}{ccc|c} 2 & 1 & 3 & 1 \\ 0 & -1 & 2 & 2 \\ 1 & 0 & -1 & -2 \end{array} \right] \xrightarrow{\textcircled{1}-2\times\textcircled{3}} \left[\begin{array}{ccc|c} 0 & 1 & 5 & 5 \\ 0 & -1 & 2 & 2 \\ 1 & 0 & -1 & -2 \end{array} \right] \xrightarrow{\textcircled{2}+\textcircled{1}} \left[\begin{array}{ccc|c} 0 & 1 & 5 & 5 \\ 0 & 0 & 7 & 7 \\ 1 & 0 & -1 & -2 \end{array} \right]$$

$$\xrightarrow{\textcircled{2}\times(1/7)} \left[\begin{array}{ccc|c} 0 & 1 & 5 & 5 \\ 0 & 0 & 1 & 1 \\ 1 & 0 & -1 & -2 \end{array} \right] \xrightarrow[\textcircled{3}+\textcircled{2}]{\textcircled{1}-5\times\textcircled{2}} \left[\begin{array}{ccc|c} 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 1 \\ 1 & 0 & 0 & -1 \end{array} \right] \xrightarrow{\textcircled{1}\leftrightarrow\textcircled{3}} \left[\begin{array}{ccc|c} 1 & 0 & 0 & -1 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 1 \end{array} \right]$$

$$\therefore \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix} = \begin{bmatrix} -1 \\ 0 \\ 1 \end{bmatrix}$$

$$(4) \left[\begin{array}{ccc|c} 2 & 3 & 0 & 4 \\ 1 & -1 & 1 & 1 \\ 3 & 1 & -3 & -2 \end{array} \right] \xrightarrow[\textcircled{3}-3\times\textcircled{2}]{\textcircled{1}-2\times\textcircled{2}} \left[\begin{array}{ccc|c} 0 & 5 & -2 & 2 \\ 1 & -1 & 1 & 1 \\ 0 & 4 & -6 & -5 \end{array} \right] \xrightarrow{\textcircled{1}-\textcircled{3}} \left[\begin{array}{ccc|c} 0 & 1 & 4 & 7 \\ 1 & -1 & 1 & 1 \\ 0 & 4 & -6 & -5 \end{array} \right]$$

$$\xrightarrow[\textcircled{3}-4\times\textcircled{1}]{\textcircled{2}+\textcircled{1}} \left[\begin{array}{ccc|c} 0 & 1 & 4 & 7 \\ 1 & 0 & 5 & 8 \\ 0 & 0 & -22 & -33 \end{array} \right] \xrightarrow[\textcircled{3}\times(-1/22)]{\textcircled{2}\times 2} \left[\begin{array}{ccc|c} 0 & 1 & 4 & 7 \\ 2 & 0 & 10 & 16 \\ 0 & 0 & 2 & 3 \end{array} \right] \xrightarrow[\textcircled{2}-5\times\textcircled{3}]{\textcircled{1}-2\times\textcircled{2}} \left[\begin{array}{ccc|c} 0 & 1 & 0 & 1 \\ 2 & 0 & 0 & 1 \\ 0 & 0 & 2 & 3 \end{array} \right]$$

$$\xrightarrow{\textcircled{3}, \textcircled{2}\times(1/2)} \left[\begin{array}{ccc|c} 0 & 1 & 0 & 1 \\ 1 & 0 & 0 & 1/2 \\ 0 & 0 & 1 & 3/2 \end{array} \right] \xrightarrow{\textcircled{1}\leftrightarrow\textcircled{2}} \left[\begin{array}{ccc|c} 1 & 0 & 0 & 1/2 \\ 0 & 1 & 0 & 1 \\ 0 & 0 & 1 & 3/2 \end{array} \right] \quad \therefore \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix} = \begin{bmatrix} 1/2 \\ 1 \\ 3/2 \end{bmatrix}$$

P. 22 3.

$$\left[\begin{array}{cc|c} 1 & 0 & 1 \\ 0 & 1 & 2 \end{array} \right] \xrightarrow{\textcircled{2} \times (-1)} \left[\begin{array}{cc|c} 1 & 0 & 1 \\ 0 & -1 & -2 \end{array} \right] \xrightarrow{\textcircled{1} \leftrightarrow \textcircled{2}} \left[\begin{array}{cc|c} 0 & -1 & -2 \\ 1 & 0 & 1 \end{array} \right]$$

$$\xrightarrow{\textcircled{1} - 2 \times \textcircled{2}} \left[\begin{array}{cc|c} 0 & -1 & -2 \\ 1 & 2 & 5 \end{array} \right] \xrightarrow{\textcircled{1} + 2 \times \textcircled{2}} \left[\begin{array}{cc|c} 2 & 3 & 8 \\ 1 & 2 & 5 \end{array} \right]$$